

A fair coin is tossed four times. Let  $X$  denote the number of heads on the first toss,  $Y$  the number of heads on the first two tosses, and let  $Z$  denote the total number of heads in four tosses.

1) Find  $f_{XYZ}(0, 1, 2)$ .

1 point

For 0 heads on first toss,  
1 head on first 2 toss and  
2 total heads

$\Rightarrow$  Possible combinations are = T H H T, T H T H

$$\Rightarrow f_{XYZ}(0, 1, 2) = 2 \left( \frac{1}{16} \right) = \frac{1}{8}$$

Q) Find  $f_{XYZ}(0, 1, 4)$

$\Rightarrow$  Possible combinations = None

Total toss = 4

if 0 heads on first toss

$\Rightarrow$  it must be tails, but total heads is 4  
which is contradicting

Q) Find  $f_{XYZ}(1, 1, 3)$

$\Rightarrow$  Possible combinations = H T H H

$$\Rightarrow f_{XYZ}(1, 1, 3) = \frac{1}{16}$$